



FIG. 1

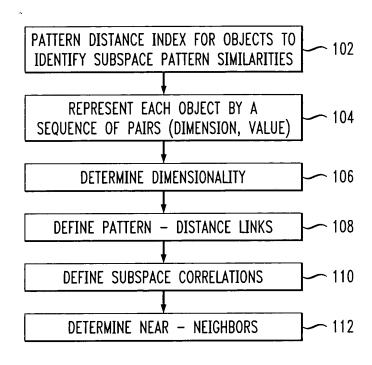


FIG. 2

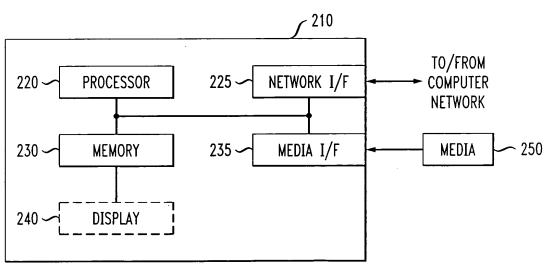


FIG. 3

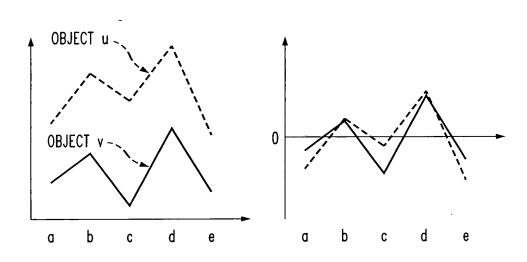


FIG. 4

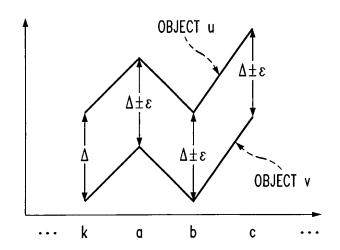


FIG. 5

f(u,i)	$f(u,i)$, where $u\in\{\#1,\ \#2\}$ and $i=1,\ 4$				
$(c_1, 0),$	$(c_2, -3),$ $(c_2, 0),$	$(c_3, 4),$	$(c_4, -1),$ $(c_4, 2),$ $(c_4, -2),$ $(c_4, 0),$	$(c_5, -4)$	
(c ₁ , 0),	$(c_2, -3),$ $(c_2, 0),$	$(c_3, 1),$ $(c_3, 4),$ $(c_3, 0),$	$(c_4, -1),$ $(c_4, 2),$ $(c_4, -2),$ $(c_4, 0),$	$(c_5, 2)$ $(c_5, 5)$ $(c_5, 1)$ $(c_5, 3)$	

FIG. 6

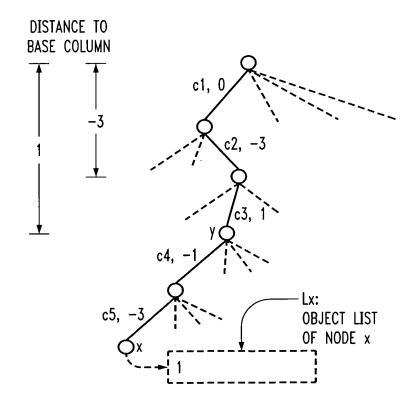


FIG. 7

```
Input: T: a trie built on D
S: a subspace defined by a continuous column set \{c_i, c_{i+1}, ..., c_k\}
q = (c_1, v_1), ..., (c_n, v_n): a query object \in: pattern threshold

Output: near-neighbors of q in subspace S

n \leftarrow \text{root of } T; search(n, S);

Function search(x, S) if S = \emptyset then

output the descendents of x;

else

assume S = \{c_j, c_{j+1}, ..., c_k\}; for x's child node y under edge labeled (c_j, v) where v \in [(v_j - v_i) - \in, (v_j - v_i) + \in] do

search (y, \{c_{j+1}, ..., c_k\});
```

FIG. 8

```
Input: D: objects in multi-dimensional space A
Output: PD-Index of D

for each u \in D do

insert f(u, i), 1 \le i < |A| into a trie; (Eq 5)

for each node x encountered in a depth-first traversal of the trie do

label node x by \langle n_x, s_x \rangle;
let (c, d) be the arc that points to x;
append \langle n_x, s_x \rangle to pattern-distance link (c, d);
```

FIG. 9A

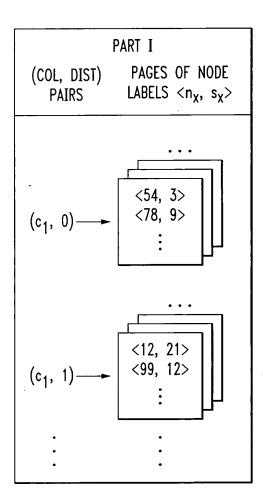


FIG. 9B

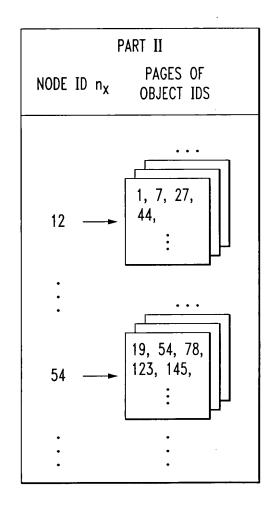
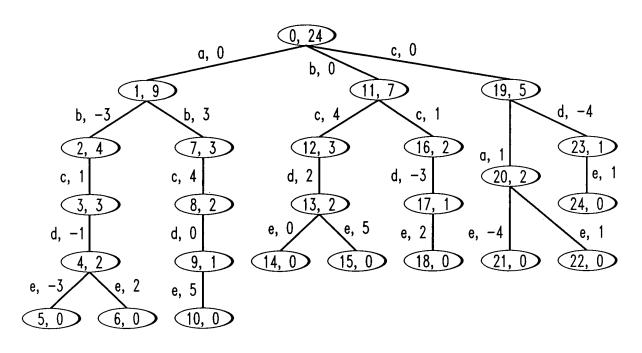


FIG. 10

```
Input: q: a query object, S: a given subspace
        €: pattern threshold
Output: q's near-neighbors in subspace S
let (c_1, v_1), ..., (c_{|S|}, v_{|S|}) be q's projection on S;
x \leftarrow \text{the node under arc}(c_1, 0);
search(x, 2);
Function search(x, i)
if i \leq |S| then
   for pattern distance link I of (c_i, v), where v \in [v_i -
   v_{\mathrm{l}} - \in, \ v_{i} - v_{\mathrm{l}} + \in ] \ \mathbf{do}
       /* perform a binary search on I */
       for all node r \in I and n_r \in [n_x, n_x + s_x] do
             search(r, i + 1);
        end
    end
else
    output objects in L_x, x = v_s, ..., v_m
end
```

FIG. 11



NODE 5 6 10 14 15 18 21 22 24 OBJS {1} {2} {3,4} {1} {2} {3,4} {1} {2} {3,4}

FIG. 12

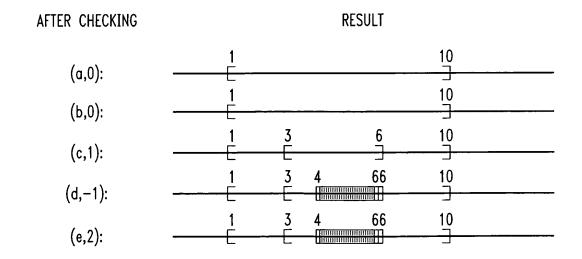
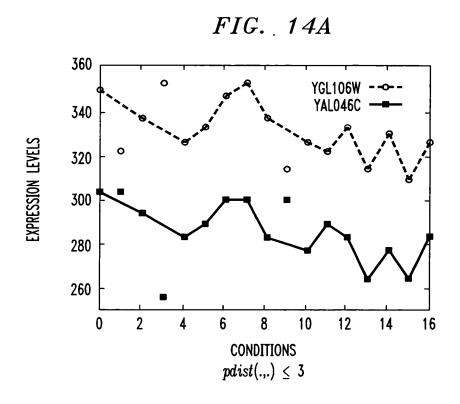
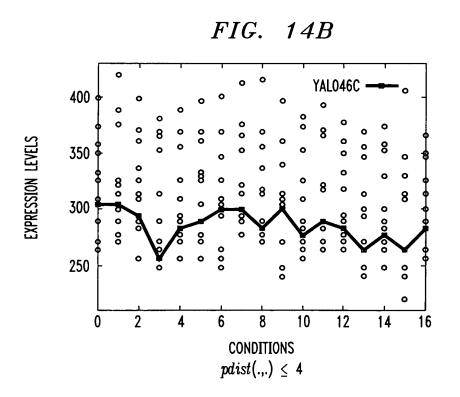
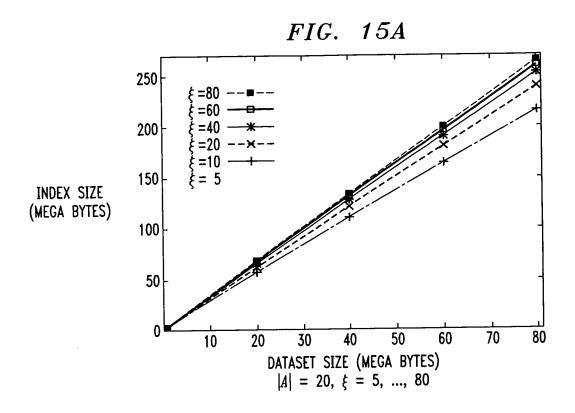


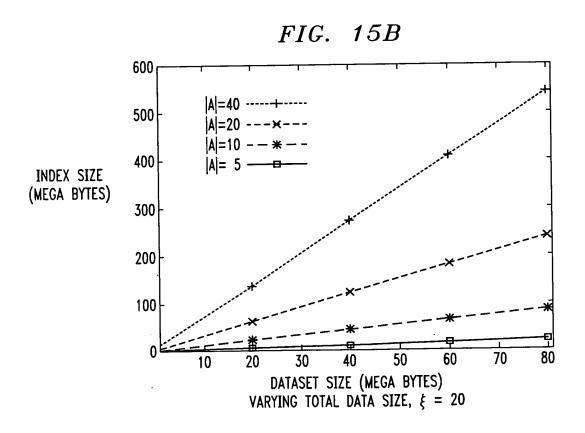
FIG. 13

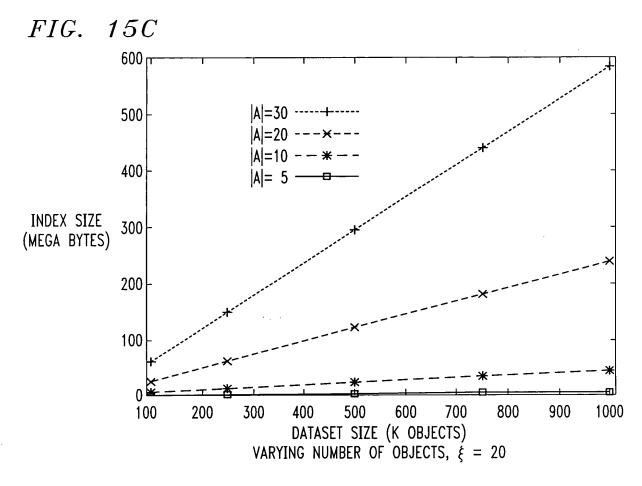
```
Input: q = (c_1, v_1), \ldots, (c_n, v_n): a query object
        r: distance threshold, \in: pattern tolerance
        F: index file for D
Output: NN(q, r)
for i = 1, ..., r + 1 do
    R \leftarrow \text{the range of the (only) node in link } (c_i, 0);
    j \leftarrow i + 1;
    while R \neq \Phi and j \leq |A| do
       search link (c_j, v) for nodes inside any range of R, where v \in [v_j - v_i - \epsilon, v_j - v_i + \epsilon];
        update R by adding the ranges of those nodes;
        if a region s of R is inside |A| - r brackets then
              output objects in L_x where x \in s;
              eliminate s from R;
        end
        if a region s of R is inside less than r - j brackets
        then
              eliminate the region from s;
        j \leftarrow j + 1;
    end
end
```

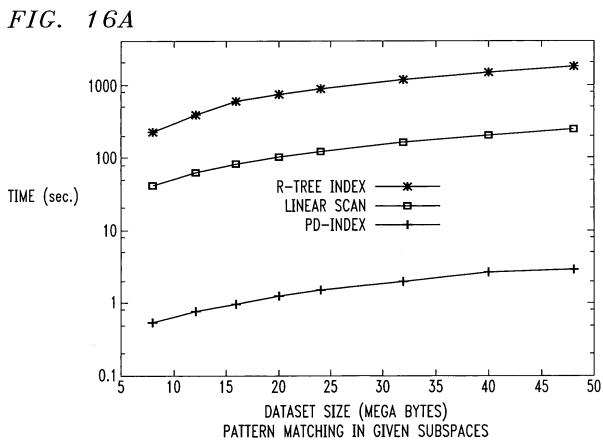




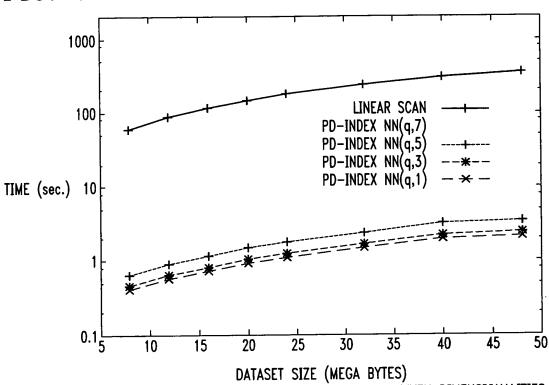












NEAR-NEIGHBOR SEARCH IN SUBSPACES BEYOND GIVEN DIMENSIONALITIES

FIG. 16C

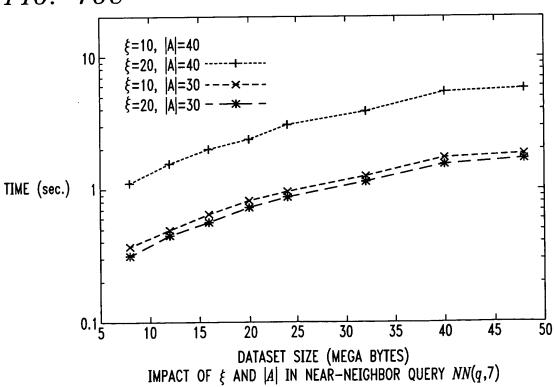


FIG. 17A

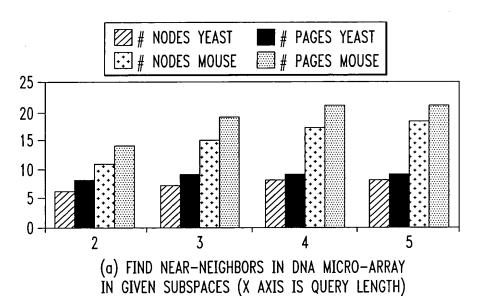


FIG. 17B

